

# PHI 120 – Introductory Logic

## Review of the Rules

**There are 10 Rules:**

<i>Elimination Rules</i> allows you to break up a (binary) connective	<i>Introduction Rules</i> allows you to build the (binary) connective
• <b>&amp;E (ampersand Elimination)</b>	• <b>&amp;I (ampersand Introduction)</b>
• <b>vE (wedge Elimination)</b>	• <b>vI (wedge Introduction)</b>
• <b>-&gt;E (arrow Elimination)</b>	• <b>-&gt;I (arrow Introduction)</b>
• <b>&lt;-&gt;E (double arrow Elimination)</b>	• <b>&lt;-&gt;I (double arrow Introduction)</b>
<b>A (Rule of Assumption)</b>	
<b>RAA (Reductio ad absurdum)</b>	

**Number and Kind of Premises (what is the conclusion of each rule?)**

1 PREMISE RULES	2 PREMISE RULES
<ul style="list-style-type: none"> <li>• <b>&amp;E (ampersand Elimination)</b> <ul style="list-style-type: none"> <li>• a conjunction</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• <b>&amp;I (ampersand Introduction)</b> <ul style="list-style-type: none"> <li>• any kind of sentence (i.e., one of the conjuncts)</li> <li>• any kind of sentence (i.e., one of the conjuncts)</li> </ul> </li> </ul>
<ul style="list-style-type: none"> <li>• <b>vI (wedge Introduction)</b> <ul style="list-style-type: none"> <li>• any kind of sentence (i.e., one of the disjuncts)</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• <b>vE (wedge Elimination)</b> <ul style="list-style-type: none"> <li>• a disjunction</li> <li>• denial of one of the disjuncts</li> </ul> </li> </ul>
<ul style="list-style-type: none"> <li>• <b>-&gt;I (arrow Introduction)</b> <ul style="list-style-type: none"> <li>• the consequent of the conditional                             <ul style="list-style-type: none"> <li>• the antecedent is the discharged assumption</li> </ul> </li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• <b>-&gt;E (arrow Elimination)</b> <ul style="list-style-type: none"> <li>• a conditional</li> <li>• antecedent of the conditional</li> </ul> </li> </ul>
<ul style="list-style-type: none"> <li>• <b>&lt;-&gt;E (double arrow Elimination)</b> <ul style="list-style-type: none"> <li>• a biconditional</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• <b>&lt;-&gt;I (double arrow Introduction)</b> <ul style="list-style-type: none"> <li>• a conditional (<math>\Phi \rightarrow \Psi</math>)</li> <li>• the mirror conditional (<math>\Psi \rightarrow \Phi</math>)</li> </ul> </li> </ul>
<i>NB: The Assumption Rule does not have any premises</i>	<ul style="list-style-type: none"> <li>• <b>RAA (Reductio ad absurdum)</b> <ul style="list-style-type: none"> <li>• any sentence (<math>\Phi</math>)</li> <li>• its contradiction (<math>\sim\Phi</math>)                             <ul style="list-style-type: none"> <li>• allows you to discharge any assumption in the proof</li> </ul> </li> </ul> </li> </ul>

**Strategy of ->I:**

<ol style="list-style-type: none"> <li>1) Assume the antecedent of conclusion</li> <li>2) Generate the consequent (i.e., as a conclusion)</li> <li>3) Apply -&gt;I rule to generate the conditional</li> </ol>
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**Strategy of RAA:**

<ol style="list-style-type: none"> <li>1) Assume the denial of the conclusion</li> <li>2) Generate a contradiction</li> <li>3) Use RAA to deny (eventually) assumption in step 1</li> </ol>
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